

Resolution of Vectors into Rectangular Components

Example 1: An airplane lifts off at 500km/h at a 35° angle to the ground. How fast is the plane climbing into the air? How fast is the plane moving relative to the ground?

Ground speed:

$$\cos 35 = \frac{x}{500}$$

$$x = 500 \cos 35$$

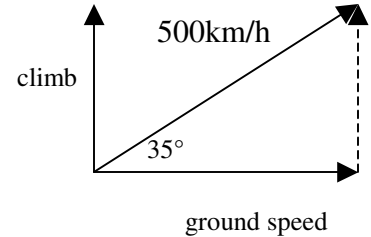
$$x \doteq 410$$

Climb:

$$\sin 35 = \frac{x}{500}$$

$$x = 500 \sin 35$$

$$x \doteq 287$$

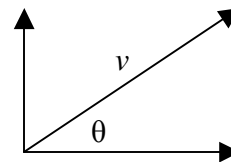


The plane is moving forward at 410km/h and rising at 287km/h.

Any vector can be resolved into **rectangular components**.

The horizontal component is $|\vec{v}| \cos \theta$.

The vertical component is $|\vec{v}| \sin \theta$.



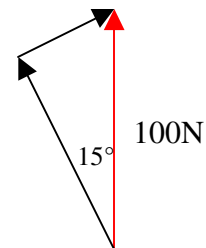
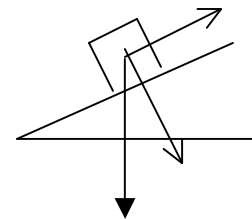
Example 2: A box weighing 100N is resting on a ramp with an incline of 15° . Resolve the weight into rectangular components that keep the box at rest.

The weight pulls straight down.

The box is held in place by two vector components:
a force perpendicular to the ramp, \vec{n} , and the force of friction, \vec{f} , parallel to the ramp.

$$\vec{n} = 100 \cos 15 = 96.6$$

$$\vec{f} = 100 \sin 15 = 25.9$$



Homework: pg. 48 # 1, 3, 7, 10, 11, 12, 13, 16