

## Surface Area

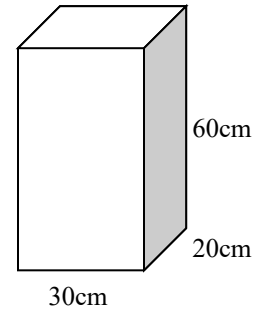
Demo: Packing Explorer (smart board)

The key to determining surface area is being able to identify all the faces of the shape and total the appropriate areas.

Example 1: Determine the surface area of the following box.

$$\begin{array}{lll} A_{\text{front}} = l \times w & A_{\text{side}} = l \times w & A_{\text{top}} = l \times w \\ = 30 \times 60 & = 20 \times 60 & = 30 \times 20 \\ = 1800 & = 1200 & = 600 \end{array}$$

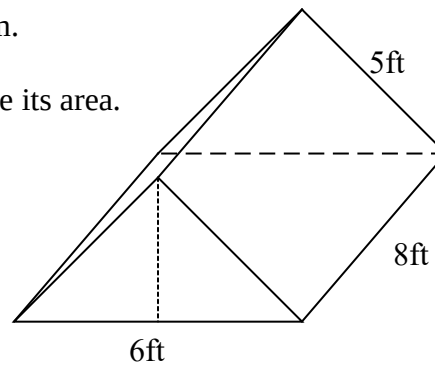
$$\begin{aligned} SA &= 2(1800) + 2(1200) + 2(600) \\ SA &= 3600 + 2400 + 1200 \\ SA &= 7200 \end{aligned}$$



Example 2: Determine the surface area of the prism.

First, we need the height of the triangle to determine its area.

$$\begin{aligned} a^2 + b^2 &= c^2 \\ 3^2 + h^2 &= 5^2 \\ h^2 &= 25 - 9 \\ h^2 &= 16 \\ h &= 4 \end{aligned}$$



$$\begin{aligned} A_{\text{front}} &= \frac{bh}{2} \\ &= \frac{(6)(4)}{2} = 12 \end{aligned}$$

$$\begin{aligned} A_{\text{side}} &= l \times w \\ &= 8 \times 5 \\ &= 40 \end{aligned}$$

$$\begin{aligned} A_{\text{bottom}} &= l \times w \\ &= 8 \times 6 \\ &= 48 \end{aligned}$$

$$\begin{aligned} SA &= 2(12) + 2(40) + 48 \\ SA &= 24 + 80 + 48 \\ SA &= 152 \end{aligned}$$

Example 3: Determine the surface area of the tin.

For the top and bottom, we have circles, so:

$$\begin{aligned}A_{\text{top}} &= \pi r^2 \\ &= \pi (5)^2 \\ &= 78.54\end{aligned}$$

For the rest of the tin, imagine peeling a label off a soup tin.

The width of the label is the same as the height of the can. The length of the label is the distance around the outside of the can – that is, the perimeter of the circle.

$$\begin{aligned}A_{\text{label}} &= l \times w \\ &= (2\pi r)(h) \\ &= 2\pi (5)(12) \\ &= 376.99\end{aligned}$$

$$SA = 2(78.54) + 376.99 = 534.07 \text{ cm}^2$$

