

Solving Right Triangles with Trig Ratios

Using Trigonometry to Determine Side Lengths

Need: a known angle (but **not** the right angle) and a side length

You must select an appropriate ratio based on *side you know* and the *side you want*.

Example 1: Determine the missing side lengths of the triangle shown.

We'll start with the **opposite** side.

We know the **adjacent** side, so we will use the **tangent** ratio.

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan 35 = \frac{x}{14}$$

$$14 \tan 35 = x$$

$$14(0.7002...) = x$$

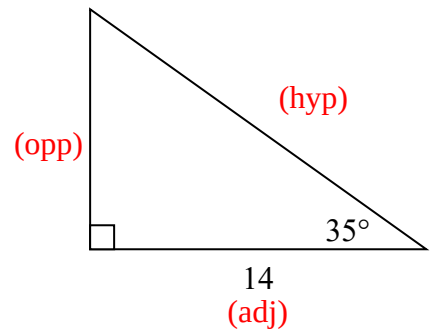
$$x \approx 9.8$$

Fill in what you know.

Multiply both sides by 14 to clear the fraction.

Use a calculator to get $\tan 35$.

The opposite side is about 9.8.



Next, let's do the **hypotenuse**. We know the **adjacent** side, so we will use the **cosine** ratio.

$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\cos 35 = \frac{14}{y}$$

$$y \cos 35 = 14$$

$$y = \frac{14}{\cos 35}$$

$$y = \frac{14}{(0.8192...)} \\ y \approx 17.1$$

Fill in what you know.

Multiply both sides by y to clear the fraction.

Divide both sides by $\cos 35$ to isolate y .

The hypotenuse is about 17.1.

Using Trigonometry to Determine Angles

Need: two sides in a right-angled triangle.

You must select the appropriate ratio based on which *sides you know*.

Example 2: Determine the value of θ .

We know the **opposite** and **hypotenuse**, so we use **sine**.

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

$$\sin \theta = \frac{3}{5}$$

$$\sin \theta = 0.6$$

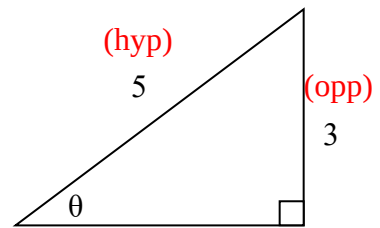
$$\theta = \sin^{-1} 0.6$$

$$\theta \approx 36.9$$

Fill in what you know.

Change the fraction into a decimal.

Use the **sine inverse** on you calculator to get the angle.



Solving Triangles

To solve a triangle means to determine all missing sides and angles.

Example 3: Solve the triangle.

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

$$\sin 28 = \frac{x}{12}$$

$$12 \sin 28 = x$$

$$12(0.469471562 \dots) = x$$

$$5.6 \approx x$$

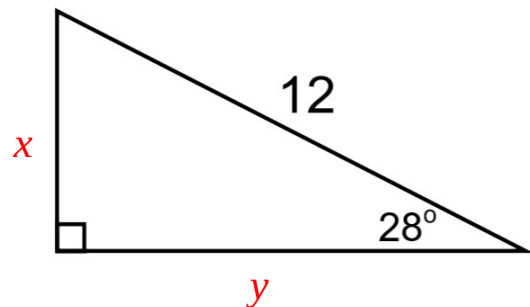
$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\cos 28 = \frac{y}{12}$$

$$12 \cos 28 = y$$

$$12(0.88294759 \dots) = y$$

$$10.6 \approx y$$



For the remaining angle, we know the angles sum to 180, so $180 - 90 - 28 = 62$.

Practice: pg. 404 #5 – 7, 10, 13, 14